NAME:

- 1. A small plane is flying north in calm air at 300 km/h when it is hit by a horizontal crosswind blowing northeast at 55 km/h and a 32 km/h downdraft.
 - (a) 10 pts. Find the resulting velocity and speed of the plane.
 - (b) <u>5 pts.</u> To the nearest degree, what is the angle (with respect to the horizontal) of the plane's descent?
- 2. 10 pts. Let $\mathbf{u} = \langle 1, 1 \rangle$ and $\mathbf{v} = \langle -2, 1 \rangle$. For arbitrary numbers a and b, express $\langle a, b \rangle$ as a linear combination of \mathbf{u} and \mathbf{v} .
- 3. 10 pts. Find an equation of the sphere passing through p = (-4, 2, 3) and q = (0, 2, 7) with its center at the midpoint of \overline{pq} .
- 4. 10 pts. Find the values of x and y such that the points (1,2,3), (4,7,1) and (x,y,9) are collinear.
- 5. 10 pts. each Let $\mathbf{u} = \langle 2, -1, 0 \rangle$ and $\mathbf{v} = \langle 4, -8, 3 \rangle$.
 - (a) Find the angle between \mathbf{u} and \mathbf{v} to the nearest tenth of a degree.
 - (b) Find $\operatorname{proj}_{\mathbf{v}} \mathbf{u}$, the orthogonal projection of \mathbf{u} onto \mathbf{v} .
- 6. 10 pts. Find the area of the parallelogram that has two adjacent sides given by $\mathbf{u} = \langle -3, 0, 2 \rangle$ and $\mathbf{v} = \langle 1, 1, 1 \rangle$.
- 7. 10 pts. Find a parametrization for the line through (-3, -3, 8) that is perpendicular to both the y-axis and $\mathbf{u} = \langle 0, 3, -5 \rangle$.
- 8. 10 pts. Determine whether the lines are parallel, intersecting, or skew:

 $\mathbf{r}(t) = \langle 5 + 2t, 3 + 3t, 1 - t \rangle, \quad \mathbf{R}(s) = \langle 13 - 3s, 13 - 4s, 4 - 2s \rangle.$

If they intersect, find the point(s) of intersection.

- 9. 10 pts. Given that $\mathbf{r}'(t) = \langle \cos t, 1 2e^{-t}, 1 2e^t \rangle$ and $\mathbf{r}(0) = \langle 1, 1, 1 \rangle$, find the function \mathbf{r} .
- 10. 10 pts. Find the speed associated with the trajectory

$$\mathbf{r}(t) = \langle 5\cos t^2, 5\sin t^2, 12t^2 \rangle,$$

and then find the length of the trajectory on the interval $0 \le t \le 2$.

11. 15 pts. Find the curvature κ of the curve $\mathbf{r}(t) = \langle t, t^2, t^2/2 \rangle$, and then find the point on the curve where the curvature attains a maximum. What is the maximum curvature value?