Math 242 Fall 2015 Exam 1

NAME:

- 1. 10 pts. If p = (-4, 1) and q = (3, -5), find two vectors parallel to \vec{pq} with length 10.
- 2. 10 pts. Three forces with magnitudes of 400 newtons, 280 newtons, and 350 newtons act on an object at angles of -30° , 45° , and -135° with the positive *x*-axis, respectively. Find the magnitude and direction of the resultant force **F**.
- 3. 10 pts. A remote sensing probe falls vertically with a terminal velocity of 60 m/s when it encounters a horizontal crosswind blowing north at 6 m/s and an updraft blowing vertically at 10 m/s. Find the magnitude and direction of the resulting velocity **v** relative to the ground.
- 4. 10 pts. Find the equation of the sphere passing through points p = (1, 0, 5) and q = (2, 3, 9), with center at the midpoint of the sequent \overline{pq} .
- 5. To pts. each Let $\mathbf{u} = \langle 2, -1, 9 \rangle$ and $\mathbf{v} = \langle -2, 4, 3 \rangle$.
 - (a) Find the angle between \mathbf{u} and \mathbf{v} to the nearest tenth of a degree.
 - (b) Find $\operatorname{proj}_{\mathbf{v}} \mathbf{u}$, the orthogonal projection of \mathbf{u} onto \mathbf{v} .
- 6. 10 pts. Find the components of the vertical force $\mathbf{F} = \langle 0, -12 \rangle$ in the directions parallel to and normal to the plane that makes an angle of $\pi/6$ with the positive x-axis.
- 7. 10 pts. Find the area of the parallelogram that has two adjacent sides given by $\mathbf{u} = \langle -3, 0, 2 \rangle$ and $\mathbf{v} = \langle 1, 1, 1 \rangle$.
- 8. 10 pts. Find a parametrization for the line through the point (-3, 4, 2) that is perpendicular to both $\mathbf{u} = \langle 1, 1, -5 \rangle$ and $\mathbf{v} = \langle 0, 4, 0 \rangle$.
- 9. 10 pts. Find a parametrization for the tangent line to the curve

$$\mathbf{r}(t) = \langle 3t - 1, 7t + 2, t^2 \rangle$$

at the point corresponding to t = 1, making sure the orientation of the line is the same as the direction of the tangent vector at that point.

10. 10 pts. Find the length of the curve

$$\mathbf{r}(t) = \langle \cos t + \sin t, \cos t - \sin t \rangle, \quad t \in [0, 2\pi].$$

11. 10 pts. Find the curvature of the curve

$$\mathbf{r}(t) = \langle \sqrt{3}\sin t, \sin t, 2\cos t \rangle.$$