

1. 10 pts. Given that  $f(x) = 2x^3 + x - 12$ , find  $(f^{-1})'(6)$ .
  
2. 10 pts. Find all the inverses associated with  $f(x) = (x - 4)^2$ , and state their domains.
  
3. 10 pts. each Find the derivative of each function.
  - (a)  $f(x) = \ln(e^{2x} + 3)$
  - (b)  $g(x) = x^{\ln(x^3)}$
  - (c)  $h(x) = (\tan x)^{\cos x}$
  - (d)  $k(x) = 7 \log_3(4 - x^5)$
  - (e)  $\ell(x) = \sin^{-1}(e^{-2x})$
  - (f)  $p(x) = \cot^{-1}(\sqrt{x})$

4. 10 pts. each Determine each indefinite integral.

- (a)  $\int (3e^{-8x} - 8e^{11x}) dx$
- (b)  $\int \frac{4}{3 - 10x} dx$
- (c)  $\int x^3 9^{x^4} dx$

5. 10 pts. each Evaluate each definite integral.

- (a)  $\int_1^{3e} \frac{e^{\ln(x)}}{2x} dx$
- (b)  $\int_2^{2\sqrt{3}} \frac{5}{z^2 + 4} dz$

6. 10 pts. Evaluate the limit using L'Hôpital's Rule:

$$\lim_{x \rightarrow \infty} \left( \frac{2}{3x} \right)^{8/x}$$

7. 10 pts. Use limit methods to determine which of the two functions grows faster:  $x^{20}$ ,  $1.001^x$ .

## FORMULAS & DEFINITIONS

1.  $\theta = \tan^{-1} x \Leftrightarrow x = \tan \theta$ , for  $\theta \in (-\pi/2, \pi/2)$
2.  $\theta = \cot^{-1} x \Leftrightarrow x = \cot \theta$ , for  $\theta \in (0, \pi)$
3.  $\theta = \sec^{-1} x \Leftrightarrow x = \sec \theta$ , for  $\theta \in [0, \pi/2) \cup (\pi/2, \pi]$
4.  $\theta = \csc^{-1} x \Leftrightarrow x = \csc \theta$ , for  $\theta \in [-\pi/2, 0) \cup (0, \pi/2]$
5.  $(b^x)' = b^x \ln b$ , for  $b \in (0, 1) \cup (1, \infty)$
6.  $(\log_b |x|)' = \frac{1}{x \ln b}$ , for  $x \neq 0$
7.  $(\sin^{-1} x)' = \frac{1}{\sqrt{1-x^2}}$ , for  $x \in (-1, 1)$
8.  $(\tan^{-1} x)' = \frac{1}{1+x^2}$ , for  $x \in (-\infty, \infty)$
9.  $(\sec^{-1} x)' = \frac{1}{|x|\sqrt{x^2-1}}$ , for  $x \in (-\infty, -1) \cup (1, \infty)$
10.  $\int b^x dx = \frac{1}{\ln b} b^x + c$ , for  $b \in (0, 1) \cup (1, \infty)$
11.  $\int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left( \frac{x}{a} \right) + c$ , for  $a \in (0, \infty)$
12.  $\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + c$ , for  $a \neq 0$
13.  $\int \frac{1}{x\sqrt{x^2-a^2}} dx = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + c$ , for  $a \in (0, \infty)$
14.  $\int \sin^n x dx = -\frac{\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$
15.  $\int \cos^n x dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x dx$
16.  $\int \tan^n x dx = \frac{\tan^{n-1} x}{n-1} - \int \tan^{n-2} x dx$ ,  $n \neq 1$
17.  $\int \sec^n x dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$ ,  $n \neq 1$
18.  $\int \tan x dx = -\ln |\cos x| + c = \ln |\sec x| + c$
19.  $\int \cot x dx = \ln |\sin x| + c$
20.  $\int \sec x dx = \ln |\sec x + \tan x| + c$
21.  $\int \csc x dx = -\ln |\csc x + \cot x| + c$