

1. 10 pts. Given that  $g(x) = x^5 - x^3 + 2x$ , find  $(g^{-1})'(2)$ .

2. 10 pts. each Find the derivative of each function.

(a)  $f(x) = \ln(e^{2x} + 3)$

(b)  $g(x) = x^{\ln(x^5)}$

(c)  $h(x) = (\sin x)^{\tan x}$

(d)  $k(x) = 7 \log_3(4 - x^5)$

(e)  $\ell(x) = \sec^{-1}(e^{-2x})$

(f)  $p(x) = \cot^{-1}(\sqrt{x})$

3. 10 pts. each Determine each indefinite integral.

(a)  $\int (3e^{-8x} - 8e^{11x}) dx$

(b)  $\int \frac{9}{4 - 9y} dy$

(c)  $\int x^7 8^{x^8} dx$

4. 10 pts. each Evaluate each definite integral.

(a)  $\int_1^{3e} \frac{e^{\ln(x)}}{2x} dx$

(b)  $\int_2^{2\sqrt{3}} \frac{5}{z^2 + 4} dz$

5. 10 pts. Evaluate the limit using L'Hôpital's Rule:

$$\lim_{x \rightarrow 0} (x + \cos x)^{1/3x}$$

6. 10 pts. Find the derivative, where  $\tanh$  denotes the hyperbolic tangent function.

$$f(x) = \sqrt{\tanh(5x)}.$$

7. 10 pts. Evaluate the integral.

$$\int_1^4 \frac{\tanh \sqrt{x}}{\sqrt{x}} dx.$$

## FORMULAS & DEFINITIONS

1.  $\theta = \tan^{-1} x \Leftrightarrow x = \tan \theta$ , for  $\theta \in (-\pi/2, \pi/2)$
2.  $\theta = \cot^{-1} x \Leftrightarrow x = \cot \theta$ , for  $\theta \in (0, \pi)$
3.  $\theta = \sec^{-1} x \Leftrightarrow x = \sec \theta$ , for  $\theta \in [0, \pi/2) \cup (\pi/2, \pi]$
4.  $\theta = \csc^{-1} x \Leftrightarrow x = \csc \theta$ , for  $\theta \in [-\pi/2, 0) \cup (0, \pi/2]$
5.  $(\sin^{-1} x)' = \frac{1}{\sqrt{1-x^2}}$ , for  $x \in (-1, 1)$
6.  $(\tan^{-1} x)' = \frac{1}{1+x^2}$ , for  $x \in (-\infty, \infty)$
7.  $(\sec^{-1} x)' = \frac{1}{|x|\sqrt{x^2-1}}$ , for  $x \in (-\infty, -1) \cup (1, \infty)$
8.  $\int b^x dx = \frac{1}{\ln b} b^x + c$ , for  $b \in (0, 1) \cup (1, \infty)$
9.  $\int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left( \frac{x}{a} \right) + c$ , for  $a \in (0, \infty)$
10.  $\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + c$ , for  $a \neq 0$
11.  $\int \frac{1}{x\sqrt{x^2-a^2}} dx = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + c$ , for  $a \in (0, \infty)$
12.  $\int \sin^n x dx = -\frac{\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$
13.  $\int \cos^n x dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x dx$
14.  $\int \tan^n x dx = \frac{\tan^{n-1} x}{n-1} - \int \tan^{n-2} x dx$ ,  $n \neq 1$
15.  $\int \sec^n x dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$ ,  $n \neq 1$
16.  $\int \tan x dx = -\ln |\cos x| + c = \ln |\sec x| + c$
17.  $\int \cot x dx = \ln |\sin x| + c$
18.  $\int \sec x dx = \ln |\sec x + \tan x| + c$
19.  $\int \csc x dx = -\ln |\csc x + \cot x| + c$