

1. 10 pts. For the function $f(x) = x^2 - 4x - 3$, $x > 2$, use the Inverse Function Theorem to find the slope of the line tangent to the graph of f^{-1} at the point $(-3, 4)$.

2. 10 pts. each Find the derivative of each function.

(a) $f(x) = \frac{\ln x}{x}$

(b) $g(x) = \left(4 + \frac{2}{x}\right)^{3x}$

(c) $h(t) = (\sin t)^{\sin t}$

(d) $r(x) = \log_9 \sqrt{3x}$

(e) $\varphi(z) = \cos^{-1}(\ln z)$

(f) $y = \operatorname{sech}^4(\ln x)$

3. 10 pts. Find the points on the graph of $y = (x^2)^x$, if any, where the tangent line is horizontal.

4. 10 pts. each Determine each indefinite integral.

(a) $\int \frac{e^x}{4e^x + 6} dx$

(b) $\int \left(\frac{3}{p-6} - \frac{4}{8p+1} \right) dp$

(c) $\int x^7 8^{x^8} dx$

(d) $\int \frac{\sinh t}{1 + \cosh t} dt.$

5. 10 pts. each Evaluate each definite integral.

(a) $\int_1^2 (1 + \ln x)x^x dx$

(b) $\int_1^{\sqrt{2}} y 2^{y^2} dy$

6. 10 pts. Evaluate the limit using L'Hôpital's Rule: $\lim_{x \rightarrow 1^+} x^{1/(2-2x)}$

FORMULAS & DEFINITIONS

FORMULAS

- $\tan x = y \Leftrightarrow \tan^{-1} y = x$, for $x \in (-\pi/2, \pi/2)$
- $\cot x = y \Leftrightarrow \cot^{-1} y = x$, for $x \in (0, \pi)$
- $\sec x = y \Leftrightarrow \sec^{-1} y = x$, for $x \in [0, \pi/2) \cup (\pi/2, \pi]$
- $\csc x = y \Leftrightarrow \csc^{-1} y = x$, for $x \in [-\pi/2, 0) \cup (0, \pi/2]$
- $(\sin^{-1} x)' = \frac{1}{\sqrt{1-x^2}}$, $(\tan^{-1} x)' = \frac{1}{1+x^2}$, $(\sec^{-1} x)' = \frac{1}{|x|\sqrt{x^2-1}}$
- $\int a^x dx = \frac{a^x}{\ln a} + c$
- $\int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1}\left(\frac{x}{a}\right) + c$
- $\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) + c$
- $\int \frac{1}{x\sqrt{x^2-a^2}} dx = \frac{1}{a} \sec^{-1}\left|\frac{x}{a}\right| + c$
- $\int \sin^n x dx = -\frac{\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$
- $\int \cos^n x dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x dx$
- $\int \tan^n x dx = \frac{\tan^{n-1} x}{n-1} - \int \tan^{n-2} x dx$
- $\int \sec^n x dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$
- $\int \tan x dx = \ln |\sec x| + c$, $\int \cot x dx = \ln |\sin x| + c$
- $\int \sec x dx = \ln |\sec x + \tan x| + c$, $\int \csc x dx = -\ln |\csc x + \cot x| + c$