

- Let  $f(x) = \sqrt[5]{x}$ .
  - 10 pts. Write the equation of the line  $L$  that represents the linear approximation to  $f$  at  $x = 32$ .
  - 5 pts. Use  $L$  to estimate  $\sqrt[5]{33}$ .
- 15 pts. Show, using appropriate theorems,<sup>1</sup> that the equation  $2x - 1 - \sin x = 0$  has exactly one real root.
- 10 pts. each Determine the following indefinite integrals, using substitution where necessary.
  - $\int (3x^{-2} - 4x^2 + 1)dx$
  - $\int [\cos(4t) - \sin(t/4)]dt$
  - $\int \frac{2x^2}{\sqrt{1-4x^3}}dx$
- 10 pts. Find the solution to the initial value problem  $f'(x) = 8x - 5$ ;  $f(0) = 4$ .
- 10 pts. The velocity of an object (in meters per second) is given by  $v(t) = 1/(2t + 1)$ . Approximate the object's displacement during the time interval  $0 \leq t \leq 10$  by subdividing the interval into 5 subintervals, using the midpoint of each subinterval to compute the height of the rectangles.
- 10 pts. Identify  $f$  and express the limit as a definite integral:  $\lim_{\Delta \rightarrow 0} \sum_{k=1}^n \bar{x}_k \cos \bar{x}_k \Delta x_k$ ;  $[1, 2]$ .
- 5 pts. each Suppose  $\int_0^3 f(x)dx = 2$ ,  $\int_3^6 f(x)dx = -9$  and  $\int_3^6 g(x)dx = 5$ . Evaluate the following.
  - $\int_0^3 5f(x)dx$
  - $\int_3^6 [3f(x) - g(x)]dx$
  - $\int_6^3 [f(x) + 2g(x)]dx$
- 15 pts. Use the *definition* of the definite integral to evaluate  $\int_3^7 (4x + 6)dx$
- 10 pts. Simplify  $\frac{d}{dx} \int_9^{x^3} \sin^5(t)dt$
- 10 pts. each Evaluate with the Fundamental Theorem of Calculus, using substitution where necessary.
  - $\int_1^4 \frac{5t^6 - \sqrt{t}}{t^2} dt$
  - $\int_0^{\pi/2} \sin^2 \theta \cos \theta d\theta$
- 10 pts. Find the area of the region bounded by the curves  $f(x) = 2x^2$  and  $g(x) = x^2 + 4$
- 10 pts. Let  $\mathcal{R}$  be the region in the first quadrant bounded by the curves  $y = 4 - x^2$ ,  $y = 0$ , and  $x = 0$ . Find the volume of the solid generated by revolving  $\mathcal{R}$  about the  $x$ -axis.

<sup>1</sup>This means doodling a graph and pointing and hooting at it will not suffice.