Math 125 Summer 2018 Exam 2

NAME:

- 1. 10 pts. Expand $(2x-1)^6$ using the Binomial Theorem.
- 2. 10 pts. Form a polynomial function of degree 3 having zeros 0, -3, 6.
- 3. [2.5 pts. each] Let $f(x) = 18(2x-5)^4(x+3)^9$.
 - (a) List each real zero of f and its multiplicity.
 - (b) Determine whether the graph of f crosses or touches the x-axis at each x-intercept.
 - (c) Determine the maximum number of turning points on the graph of f.
 - (d) Determine the end behavior of the graph of f.
- 4. 15 pts. Let $f(x) = 2x^4 x^3 5x^2 + 2x + 2$. Use the Rational Zeros Theorem to find all the real zeros of f, then use the zeros to factor f over the real numbers.
- 5. 10 pts. Solve the equation in the real number system:

$$x^3 + \frac{3}{2}x^2 + 3x - 2 = 0.$$

6. 10 pts. The complex number 3 - 2i is a zero of

$$f(x) = x^4 - 9x^3 + 21x^2 + 21x - 130.$$

Find the remaining zeros of f.

7. 5 pts. each For the rational function

$$Q(x) = \frac{x^2}{x^2 + x - 6}$$

do the following.

- (a) Find the domain of Q.
- (b) Find the intercepts of Q.
- (c) Find all vertical asymptotes of Q.
- (d) Find the horizontal or oblique asymptote of Q.
- (e) Find all points where Q intersects its horizontal or oblique asymptote.
- (f) Sketch the graph of Q, finding additional points as needed.

8. 10 pts. each Solve each inequality algebraically.

(a)
$$3x^3 < -15x^2$$
.
(b) $\frac{(x-2)^2}{x^2-1} \ge 0$

9. 10 pts. Find the domain of the function

$$f(x) = \sqrt{\frac{x-2}{2x+5}}.$$

10. 10 pts. each Let

$$f(x) = \sqrt{x+9}$$
 and $g(x) = 1 - 7x$.

- (a) Find $f \circ g$, and state its domain.
- (b) Find $f \circ f$, and state its domain.
- 11. 10 pts. each Find the inverse of each function. (a) $f(x) = x^2 - 36, x \le 0.$ (b) $g(x) = \frac{4x - 1}{3x + 8}$