NAME:

- 1. 5 pts. each Find the exact value of each expression, or state that it is undefined.
 - (a) $\tan^{-1}\left[\tan\left(-\frac{2\pi}{3}\right)\right]$ (b) $\cos^{-1}\left[\sin\left(\frac{7\pi}{6}\right)\right]$
- 2. 10 pts. each Let $f(x) = 2 \tan x 3$ for $-\frac{\pi}{2} < x < \frac{\pi}{2}$.
 - (a) Find the inverse function f^{-1} .
 - (b) Find the range of f, and the domain and range of f^{-1} .
- 3. 10 pts. Write the trigonometric expression $\tan(\cos^{-1} u)$ as an algebraic expression in u.
- 4. 10 pts. each Solve each trigonometric equation on the interval $0 \le \theta < 2\pi$. (a) $2\cos^2\theta + \cos\theta - 1 = 0$ (b) $(\cot\theta + 1)(\csc\theta - \frac{1}{2}) = 0$
- 5. 10 pts. What are the zeros of $f(x) = 2\cos(3x) + 1$ on the interval $[0, \pi]$?
- 6. 10 pts. each Establish the identity, showing all steps.
 - (a) $\frac{\cos v}{1+\sin v} + \frac{1+\sin v}{\cos v} = 2\sec v$ (b) $\tan \theta + \cot \theta = \sec \theta \csc \theta$
- 7. 10 pts. Find the exact value of $\sin(\alpha + \beta)$ and $\tan(\alpha \beta)$ given that

$$\cos \alpha = \frac{1}{2}, \ -\frac{\pi}{2} < \alpha < 0; \ \sin \beta = \frac{1}{3}, \ 0 < \beta < \frac{\pi}{2}$$

- 8. 10 pts. each Establish the identity
 - (a) $\sec(\alpha \beta) = \frac{\sec \alpha \sec \beta}{1 + \tan \alpha \tan \beta}$ (b) $\tan(v/2) = \csc v - \cot v$
- 9. 10 pts. Solve the equation $\sin(2\theta) = \cos\theta$ on the interval $0 \le \theta < 2\pi$.
- 10. 10 pts. A 22-foot ladder leaning against a building makes a 70° angle with the ground. How far up the building does the ladder touch?

11. 10 pts. each Solve the triangle, rounding to the tenths place.

- (a) $A = 50^{\circ}, B = 30^{\circ}, a = 1.$
- (b) $a = 3, b = 4, A = 10^{\circ}$.
- (c) a = 10, b = 7, c = 8.
- 12. 15 pts. Two observers simultaneously measure the angle of elevation of a helicopter. One angle is measured as 25°, the other as 40°. If the observers are 100 meters apart and the helicopter lies over the line joining them, how high is the helicopter?

TRIGONOMETRIC IDENTITIES

 $\sin(u \pm v) = \sin u \cos v \pm \cos u \sin v$ $\cos(u \pm v) = \cos u \cos v \mp \sin u \sin v$ $\tan(u \pm v) = \frac{\tan u \pm \tan v}{1 \mp \tan u \tan v}$

 $\sin 2u = 2\sin u \cos u$ $\cos 2u = \cos^2 u - \sin^2 u$ $\tan 2u = \frac{2\tan u}{1 - \tan^2 u}$ $\sin \frac{u}{2} = \pm \sqrt{\frac{1 - \cos u}{2}}, \quad \cos \frac{u}{2} = \pm \sqrt{\frac{1 + \cos u}{2}}, \quad \tan \frac{u}{2} = \frac{\sin u}{1 + \cos u}$