Math 125 Spring 2013 Exam 3

NAME:

1. 5 pts. each Let
$$f(x) = \frac{x^2}{x^2 - x - 2}$$

- (a) Find the domain of f.
- (b) Find the intercepts of f.
- (c) Find all vertical asymptotes of f.
- (d) Find the horizontal or oblique asymptote of f.
- (e) Find all points where f intersects its horizontal or oblique asymptote.
- (f) Sketch the graph of f, finding additional points as needed.
- 2. 10 pts. each Solve the inequality. Where applicable, write the solution set in interval notation.
 - (a) $x^2 + 5x + 6 > 0$ (b) $\frac{2x+1}{x-5} \le 3$
 - (c) $x^2 + 12 < 4x$

3. 5 pts. each The compound interest formula is $A(t) = P(1 + r/n)^{nt}$. Suppose that \$750 is invested at 8% interest, compounded quarterly.

- (a) Find the function for the amount to which the investment grows after t years.
- (b) Find the amount of money in the account at time t = 5 and t = 10 years.
- 4. 5 pts. each
 - (a) Convert $p^k = 3$ to a logarithmic equation.
 - (b) Convert $\log_a M = -x$ to an exponential equation.
- 5. 10 pts. Express $\ln(x^2 9) \ln(x + 3)$ as a single logarithm, and simplify if possible.
- 6. 10 pts. each Solve the equation algebraically.

(a)
$$5^{4x-7} = 125$$

(b)
$$3^x = 2^{x-1}$$

- (c) $\log_2(10+3x) = 5$
- (d) $\log_2(x+1) + \log_2(x-1) = 3$
- 7. 10 pts. Given that $\tan \varphi = 2$, find the other five trigonometric function values.

- 8. 10 pts. Convert 67.84° to degrees, minutes, and seconds. Round to the nearest second.
- 9. 10 pts. To measure the height of a cloud at night, a vertical beam of light is directed at the cloud. From a point on the ground 75 meters away from the light source, the angle of elevation to the illuminated spot on the cloud is determined to be 62.35°. Find the height of the cloud to the nearest meter.
- 10. 10 pts. Find two positive angles and two negative angles that are coterminal with the angle 109.2°.
- 11. 10 pts. Given that $\cos \alpha = -\frac{4}{5}$ and α is an angle in Quadrant II, find the other five trigonometric function values. Give exact answers!