Math 125 Fall 2019 Exam 3

NAME:

- 1. 10 pts. Find the domain and range of the function: $f(x) = 5 + 8^{x/2}$.
- 2. 10 pts. Solve for $x: (e^4)^x \cdot e^{x^2} = e^{12}$.
- 3. 10 pts. Find the domain of the function

$$g(x) = \ln\left(\frac{3x}{2x+11}\right).$$

- 4. 10 pts. Find the exact solution to $-e^{-0.2x} = 12$.
- 5. 10 pts. The atmospheric pressure p on an object decreases with increasing altitude. Measured in millimeters of mercury (mmHg), this pressure is related to the height h (in kilometers) above sea level by the function

$$p(h) = 760e^{-0.145h}$$
.

To the nearest hundredth, find the height of an aircraft if the atmospheric pressure is 400 mmHg.

6. 10 pts. Write as a single logarithm:

$$3\log_2(x-3) - \log_2(2x-1) - \log_2(x+1).$$

- 7. 10 pts. each Solve each equation in exact form.
 - (a) $\log_6(x+4) + \log_6(x+3) = 1.$
 - (b) $(3/5)^x = 7^{1-x}$.
- 8. 10 pts. each Iodine-131 is a radioactive isotope that decays according to the function $A(t) = A_0 e^{-0.087t}$, where A_0 is the initial amount present and A(t) is the amount present at time t (in days).
 - (a) If there are initially 100 grams of iodine-131, how much is left after 11 days to the nearest tenth of a gram?
 - (b) What is the half-life of iodine-131 to the nearest hundredth of a day?
- 9. 10 pts. Convert 140.547° to degree-minute-second format, rounding to the nearest second.
- 10. 10 pts. The terminal side of the angle θ contains the point (5, -12). Find the exact value of each of the six trigonometric functions of θ .
- 11. 10 pts. Given that $\sin \theta = -2/3$ and $\pi < \theta < 3\pi/2$, find the exact value of each of the remaining trigonometric functions of θ .

- 12. 10 pts. Find the domain and range of the function $y = -4\sin(x/8) + 1$.
- 13. 10 pts. Find the domain and range of the function

$$y = -3\sec\left(\frac{3\pi}{2}x\right).$$

14. 10 pts. Write the equation of a cosine function having amplitude 4 and period $\pi/6$.