

1. 10 pts. Form a polynomial function of degree 5 that has zeros  $-2$  (with multiplicity 2) and  $4$  (with multiplicity 3).
2. Let  $f(x) = 2x^3 - 3x^2 - 17x + 30$ .
  - (a) 5 pts. List the possible rational zeros of  $f$ .
  - (b) 10 pts. Find all zeros of  $f$  using synthetic division. Give exact values.
  - (c) 5 pts. Fully factor  $f(x)$ .
3. 10 pts. Find all the zeros of  $p(x) = x^3 + 13x^2 + 57x + 85$ , including any complex zeros.
4. 10 pts. Find the vertical, horizontal, and oblique asymptotes, if any, of the rational function

$$r(x) = \frac{2x^2 - 5x - 12}{3x^2 - 11x - 4}.$$

5. 10 pts. each Solve each inequality algebraically.

(a)  $x^3 + 2x^2 - 3x > 0$ .

(b)  $\frac{x+2}{x-4} \geq 1$ .

6. 12 pts. Given that

$$f(x) = \frac{3}{x-1} \quad \text{and} \quad g(x) = \sqrt[3]{x},$$

find  $(f \circ g)(8)$ ,  $(g \circ f)(2)$ ,  $(f \circ f)(-3)$ , and  $(g \circ g)(-64)$ .

7. 6 pts. each Let

$$f(x) = x^2 + 4 \quad \text{and} \quad g(x) = \sqrt{x-2}.$$

- (a) Find  $f \circ g$  and its domain.
  - (b) Find  $g \circ f$  and its domain.
  - (c) Find  $g \circ g$  and its domain.
8. 10 pts. each Each function is one-to-one. Find its inverse.
  - (a)  $f(x) = x^3 + 9$ .
  - (b)  $h(x) = -\frac{2x}{x-1}$ .