

1. [10 pts.] Find the inverse for the one-to-one function $f(x) = x^3 + 7$.

2. [20 pts.] Find the inverse for $h(x) = \frac{2x-3}{x+4}$. Also state the domain and the range of both h and h^{-1} .

3. [10 pts.] Determine analytically (not with a graph) whether the given function is linear or nonlinear. If it is linear, determine the equation of the line.

x	y
-20	-8
-10	-3
0	0
10	3
20	8

4. [10 pts. each] Consider the quadratic function $f(x) = 2x^2 - x + 2...$

- (a) Find the vertex and axis of symmetry.
(b) Write $f(x)$ in the form $a(x-h)^2 + k$. Determine the domain and range of f .

5. [10 pts.] Find the point on the line $y = x$ that is closest to the point $(-1, 2)$.¹

6. [10 pts. each] Solve each glorious inequality.

- (a) $x(x+1) > 20$
(b) $x^3 - 2x^2 - 3x < 0$
(c) $\frac{3x-5}{x+2} \leq 2$

7. [10 pts.] Construct a polynomial function f of degree 3 and having $-2, 1, 4$ as zeros.²

8. [15 pts.] Find all asymptotes for the rational function $R(x) = \frac{x^3 - 8}{x^2 - 5x + 6}$

9. [15 pts.] Find *exactly* the real zeros of f and fully factor $f(x)$, where

$$f(x) = 2x^4 + 11x^3 - 5x^2 - 43x + 35.$$

10. [15 pts.] Construct a degree 4 polynomial function f with *real* coefficients and having zeros $3 + 2i$ (with multiplicity 1) and 4 (with multiplicity 2). Write the polynomial in standard form!

11. [15 pts.] Find the complex zeros of f and fully factor $f(x)$, where

$$f(x) = x^3 - 8x^2 + 25x - 26.$$

¹You will recall that a homework problem like this was discussed extensively one day in class.

²For 10 points extra credit: make f such that $f(5) = 16$.