

Math 120
Exam #3
Spring 2011

Name:

1. 10 pts. Write an equation in slope-intercept form for the line through $(-1, 5)$ and parallel to $3x - 5y = 1$.
2. 10 pts. Write an equation in slope-intercept form for the line through $(-2, 3)$ and perpendicular to $8x + 3y = 6$.
3. 10 pts. Explain why the relation $x = y^6$ is not a function. Also give the domain and range.
4. 10 pts. Let $f(x) = x^2 - 3x$. Find $f(-4)$ and $f(c + 2)$.
5. 10 pts. each Find the domain and range of each function.

 - (a) $xy = 2$
 - (b) $y = |x| - 8$
6. 5 pts. each Find the domain of each function (not the range).

 - (a) $\alpha(x) = \frac{x + 1}{3x - 2}$
 - (b) $\beta(x) = \sqrt{9x - 5}$
 - (c) $\gamma(x) = \sqrt{16 - x^2}$
7. 10 pts. each Refer to the functions α, β, γ in Problem 6. There is no need to simplify any of your expressions, but domains must be explicit.

 - (a) Find $\alpha - \gamma$ and its domain.
 - (b) Find $\alpha\beta$ and its domain.
 - (c) Find $\beta \circ \beta$ and its domain.
 - (d) Find $\beta \circ \gamma$ and its domain.
8. 10 pts. Let $\Omega(x) = (2x - 3)^8$. Find functions f and g such that $f \circ g = \Omega$.
9. 10 pts. Show the function $f(x) = 2x^3 - 1$ is one-to-one.
10. 10 pts. Show the function $g(x) = 3x^2 - 4$ is not one-to-one.
11. The function $f(x) = \frac{x + 1}{x - 3}$ is one-to-one.

 - (a) 10 pts. Find the inverse f^{-1} of f .
 - (b) 5 pts. Find the range of f .
 - (c) 5 pts. Find the range of f^{-1} .

EXTRA CREDIT (20 PTS.): Find the domain of

$$F(x) = \sqrt[6]{\frac{x^2 + 2x}{x - 3}}$$