

**1** Solve  $3x - 4y = 2$  for  $y$  to get  $y = \frac{3}{4}x - \frac{1}{2}$ , which shows the slope for the line given by  $3x - 4y = 2$  to be  $\frac{3}{4}$ . Since the line  $L$  through  $(-2, -7)$  is parallel to this line, its slope must also be  $\frac{3}{4}$ . So the equation for  $L$  is  $y - (-7) = \frac{3}{4}(x - (-2))$ , or

$$y = \frac{3}{4}x - \frac{11}{2}.$$

**2** Solve  $8x - 3y = 6$  for  $y$  to get  $y = \frac{8}{3}x - 2$ , which shows the slope for the line given by  $8x - 3y = 6$  to be  $\frac{8}{3}$ . Since the line  $L$  through  $(2, -4)$  is perpendicular to this line, its slope must also be  $-\frac{3}{8}$ . So the equation for  $L$  is  $y - (-4) = -\frac{3}{8}(x - 2)$ , or

$$y = -\frac{3}{8}x - \frac{13}{4}.$$

**3** Domain is  $[-6, 6]$  and range is  $[-8, 8]$ . Relation is not a function since it contains two distinct ordered pairs having the same first component value:  $(0, 8)$  and  $(0, -8)$ .

**4**  $f(-8) = (-8)^2 + \sqrt[3]{-8} = 64 + (-2) = 62$  and  $f(c) = c^2 + \sqrt[3]{c}$

**5a** Domain and range are both  $(-\infty, \infty)$

**5b** Domain is  $(-\infty, \infty)$  and range is  $[-9, \infty)$

**6a**  $\text{Dom}(\alpha) = \{x \mid x \neq \frac{2}{3}\} = (-\infty, \frac{2}{3}) \cup (\frac{2}{3}, \infty)$

**6b**  $\text{Dom}(\beta) = \{x \mid x - 5 \geq 0\} = \{x \mid x \geq 5\} = [5, \infty)$

**6c**  $\text{Dom}(\gamma) = \{x \mid 64 - x^2 \geq 0\} = \{x \mid x^2 \leq 64\} = \{x \mid -8 \leq x \leq 8\} = [-8, 8]$

**7a** By definition we have

$$(\alpha + \gamma)(x) = \alpha(x) + \gamma(x) = \frac{x+1}{3x-2} + \sqrt{64-x^2}.$$

Also

$$\text{Dom}(\alpha + \gamma) = \text{Dom}(\alpha) \cap \text{Dom}(\gamma) = [(-\infty, \frac{2}{3}) \cup (\frac{2}{3}, \infty)] \cap [-8, 8] = [-8, \frac{2}{3}) \cup (\frac{2}{3}, 8].$$

**7b** We find

$$(\alpha/\beta)(x) = \alpha(x)/\beta(x) = \frac{x+1}{3x-2} \cdot \frac{1}{\sqrt{x-5}} = \frac{x+1}{(3x-2)\sqrt{x-5}},$$

and

$$\begin{aligned}\text{Dom}(\alpha/\beta) &= \{x : x \in \text{Dom}(\alpha) \cap \text{Dom}(\beta) \text{ and } \beta(x) \neq 0\} \\ &= \{x : x \in (-\infty, \tfrac{2}{3}) \cup (\tfrac{2}{3}, \infty) \text{ and } x \in [5, \infty) \text{ and } x \neq 5\} \\ &= (5, \infty).\end{aligned}$$

**7c** We find

$$(\beta \circ \beta)(x) = \beta(\beta(x)) = \beta(\sqrt{x-5}) = \sqrt{\sqrt{x-5}-5},$$

and the domain is given by

$$\begin{aligned}\text{Dom}(\beta \circ \beta) &= \{x : x \in \text{Dom}(\beta) \text{ and } \beta(x) \in \text{Dom}(\beta)\} \\ &= \{x : x \geq 5 \text{ and } \sqrt{x-5} \geq 5\} \\ &= \{x : x \geq 5 \text{ and } x \geq 30\} \\ &= \{x : x \geq 30\} = [30, \infty).\end{aligned}$$

**7d** We find

$$(\beta \circ \gamma)(x) = \beta(\gamma(x)) = \beta(\sqrt{64-x^2}) = \sqrt{\sqrt{64-x^2}-5},$$

and the domain is given by

$$\begin{aligned}\text{Dom}(\beta \circ \gamma) &= \{x \mid x \in \text{Dom}(\gamma) \text{ and } \gamma(x) \in \text{Dom}(\beta)\} \\ &= \{x : -8 \leq x \leq 8 \text{ and } \sqrt{64-x^2} \geq 5\} \\ &= \{x : -8 \leq x \leq 8 \text{ and } x^2 \leq 39\} \\ &= \{x : -8 \leq x \leq 8 \text{ and } -\sqrt{39} \leq x \leq \sqrt{39}\} \\ &= [-\sqrt{39}, \sqrt{39}].\end{aligned}$$

**8** Let  $f(x) = 18/x^{10}$  and  $g(x) = 7 - 2x$ . Then

$$(f \circ g)(x) = f(g(x)) = f(7 - 2x) = \frac{18}{(7 - 2x)^{10}} = H(x).$$

**9** Suppose that  $f(a) = f(b)$ . Then

$$2a^3 - 1 = 2b^3 - 1 \Rightarrow 2a^3 = 2b^3 \Rightarrow a^3 = b^3 \Rightarrow a = b.$$

Therefore  $f$  is one-to-one.

**10**  $g(-1) = 0 = g(12)$

**11a** Suppose that  $f(x) = y$ . Then

$$y = \frac{4x+1}{x-10} \Rightarrow xy - 10y = 4x + 1 \Rightarrow xy - 4x = 10y + 1 \Rightarrow x = \frac{10y+1}{y-4},$$

and since  $f^{-1}(y) = x$  by definition, it follows that

$$f^{-1}(y) = \frac{10y+1}{y-4}.$$

**11b**  $\text{Ran}(f) = \text{Dom}(f^{-1}) = (-\infty, 4) \cup (4, \infty)$

**11c**  $\text{Ran}(f^{-1}) = \text{Dom}(f) = (-\infty, 10) \cup (10, \infty)$