**1a** Since

$$f(-x) = 7 - 3(-x) + 19(-x)^2 = 7 + 3x + 19x^2 \neq \pm f(x),$$

the function f is neither even nor odd.

**1b** Here 
$$g(-x) = 2(-x)^4 - |-x| = 2x^4 - |x| = g(x)$$
, so g is even.

- **2a**  $f(x) = \sqrt{x-7} + 9$
- **2b**  $f(x) = -(x-3)^2 8$
- **3a**  $7i \cdot 9i = 63i^2 = -63.$

**3b** 
$$-6i - 12i^2 = -6i + 12 = 12 - 6i$$
.

- **3c**  $(5-4i)(5-4i) = 25 40i + 16i^2 = 9 40i.$
- **3d**  $\frac{i}{3-i} \cdot \frac{3+i}{3+i} = \frac{3i+i^2}{9-i^2} = \frac{3i-1}{10} = -\frac{1}{10} + \frac{3}{10}i.$
- **4** Factoring gives t(3t-2)(t-1) = 0, and so the solution set is  $\{0, 1, \frac{2}{3}\}$ .
- 5 We have

 $x^2 + 6x = -2 \implies x^2 + 6x + 9 = -2 + 9 \implies (x+3)^2 = 7 \implies x+3 = \pm\sqrt{7},$ and so the solution set is  $\{-3 - \sqrt{7}, -3 + \sqrt{7}\}.$ 

## **6** The quadratic formula gives

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(1)}}{2(1)} = \frac{1 \pm \sqrt{-3}}{2} = \frac{1}{2} \pm \frac{\sqrt{3}}{2}i.$$

7 Factoring yields:

$$(y^2 - 16)(y^2 + 1) = 0,$$

so either  $y^2 - 16 = 0$  (giving the solutions  $\pm 4$ ) or  $y^2 + 1 = 0$  (giving the solutions  $\pm i$ ). Solution set is  $\{-4, 4, -i, i\}$ .

8 Let  $\ell$  be the length and w the width. We're given  $2\ell + 2w = 28$  and  $\ell w = 48$ , which implies (14 - w)w = 48, and hence (w - 6)(w - 8) = 0. Thus we find that w = 6, 8. When w = 6 we get  $\ell = 8$ , and vice-versa. Therefore the dimensions are 6 ft by 8 ft.

**9a** Get into vertex form:

$$f(x) = -3(x^2 - 8x) - 49 = -3(x^2 - 8x + 16) - 49 - (-3)(16) = -3(x - 4)^2 - 1$$

So f has vertex at (4, -1).

- **9b** Maximum value is f(4) = -1.
- **9c** Range:  $(-\infty, -1]$ .
- **9d** Increasing on  $(-\infty, 4)$ , decreasing on  $(4, \infty)$ .

10 Let w and  $\ell$  be the width and length of the rectangular part of the window, as in the figure:

(Note: the "outer edges" do not include the top side of the rectangle!) The radius of the semicircle is then  $\frac{1}{2}w$ . The perimeter is to be 24 ft, so

$$24 = 2\ell + w + \frac{\pi}{2}w,$$

where  $\frac{\pi}{2}w$  is half the circumference of a circle of radius  $\frac{1}{2}w$ . Now,

$$\ell = 12 - \frac{\pi + 2}{4}w.$$

Let A(w) be the function that gives the area of the window as a function of w. We have

$$A(w) = w\ell + \frac{1}{2}\pi \left(\frac{1}{2}\right)^2 = w\left(12 - \frac{\pi + 2}{4}w\right) + \frac{\pi}{8}w^2 = -\frac{\pi + 4}{8}w^2 + 12w.$$

We want to find w for which A(w) is maximal. To do this either use a formula or get vertex form:

$$A(w) = -\frac{\pi + 4}{8} \left( w - \frac{48}{\pi + 4} \right)^2 + \frac{288}{\pi + 4}$$

Thus A(w) is maximal when  $w = 48/(\pi + 4)$ . Length is then

$$\ell = 12 - \frac{\pi + 2}{4}w = 12 - \frac{\pi + 2}{4} \cdot \frac{48}{\pi + 4} = \frac{24}{\pi + 4}$$

Dimensions of the rectangular part:  $48/(\pi + 4)$  ft wide and  $24/(\pi + 4)$  ft high.

**11a** Multiply by  $x^2 - 9$  to get

$$2 + 5(x+3) = 3(x-3) \implies x = -13.$$

Solution set:  $\{-13\}$ .

**11b** Square both sides once, and then a second time:

$$(\sqrt{x+4}+2)^2 = x^2 \Rightarrow 4\sqrt{x+4} = x^2 - x - 8$$



$$\Rightarrow 16(x+4) = x^4 - 2x^3 - 15x^2 + 16x + 64$$
  
$$\Rightarrow x^4 - 2x^3 - 15x^2 = 0,$$

and so we have  $x^2(x-5)(x+3) = 0$ , and finally x = 0, 5, -3. However 0 and -3 are extraneous solutions. The solution set is  $\{5\}$ .

**11c** A square root is never equal to a negative number, so the left-hand side of the equation cannot possibly equal 0 for any value of x. There is thus no solution. Solution set:  $\emptyset$ .

**11d** We have  $5x - 3 = \pm 12$ , so  $x = (3 \pm 12)/5$ , and hence  $x = -\frac{9}{5}, 3$ . Solution set:  $\{-\frac{9}{5}, 3\}$ .

12 We have

$$\frac{1}{2t} = \frac{24b-a}{3ab} \quad \Rightarrow \quad 2t = \frac{3ab}{24b-a} \quad \Rightarrow \quad t = \frac{3ab}{2(24b-a)}.$$

13a We have

 $-16 < 6x - 4 < 16 \quad \Rightarrow \quad -12 < 6x < 20 \quad \Rightarrow \quad -2 < x < \frac{10}{3}.$ 

Solution set:  $\left(-2, \frac{10}{3}\right)$ .

**13b** Either  $x + 6 \ge 4$  or  $x + 6 \le -4$ , and so  $x \ge -2$  or  $x \le -10$ . Solution set in interval notation:  $(-\infty, -10] \cup [-2, \infty)$ .

**13c** Either 3x - 1 > 5x + 2 or 3x - 1 < -(5x + 2), giving  $x < -\frac{3}{2}$  or  $x < -\frac{1}{8}$ . Solution set:  $(-\infty, -\frac{1}{8})$ .