**1a** 
$$5x^2 - 3x - 2 = 0 \implies (5x + 2)(x - 1) = 0 \implies 5x + 2 = 0 \text{ or } x - 1 = 0, \text{ so } x = 1, -2/5$$

**1b** 
$$x^2 - 3x = 6 \implies x^2 - 3x + 9/4 = 6 + 9/4 \implies \left(x - \frac{3}{2}\right)^2 = \frac{33}{4} \implies x - \frac{3}{2} = \pm \frac{\sqrt{33}}{2} \implies x = \frac{3}{2} \pm \frac{\sqrt{33}}{2}$$

2 If w is the width of the metal sheet, then the length of the sheet is w + 10. However, the box has width w - 4 and length (w + 10) - 4 = w + 6, and the height must be 2. The volume V of the box is computed as V = 2(w - 4)(w + 6), but we're also given that V = 832. This gives us an equation: 2(w - 4)(w + 6) = 832. Hence  $w^2 + 2w - 440 = 0$ , which leads to (w + 22)(w - 20) = 0 and so w = -22, 20. Clearly the width of the original sheet can't be -22 cm, which leaves it to be 20 cm. Dimensions of sheet: 20 cm by 30 cm.

3 Let w be the width, so the length is w + 6. By the Pythagorean Theorem the length of the diagonal is  $\sqrt{w^2 + (w+6)^2}$ , which is given to be 174, so that

$$w^{2} + (w+6)^{2} = 174^{2} \implies w^{2} + 6w - 15,120 = 0 \implies (w-120)(w-126) = 0.$$

Thus the width is 120, and then the length is 126. Dimensions are 126 m  $\times$  120 m.

4	4

	Rate of Work	Time Worked	Fraction of Job Done
Emperor	$\frac{1}{280}$	t	$\frac{t}{280}$
Vader	$\frac{1}{700}$	t	$\frac{t}{700}$

Let t be the time it would take to complete the job. We get

$$\frac{t}{280} + \frac{t}{700} = 1 \implies 700t + 280t = (700)(280) \implies 980t = 196,000 \implies t = 200 \text{ hours.}$$

**5a** We have

$$x(x+2)\left(\frac{x}{x+2} + \frac{1}{x} + 3\right) = x(x+2) \cdot \frac{2}{x(x+2)} \implies x^2 + (x+2) + 3x(x+2) = 2 \implies 4x^2 + 7x = 0,$$

giving x(4x+7)=0, and finally  $x=0,-\frac{7}{4}$ . However, 0 is an extraneous solution, so the solution set is  $\left\{-\frac{7}{4}\right\}$ .

**5b**  $\sqrt{2x} = x - 4 \implies 2x = (x - 4)^2 \implies x^2 - 10x + 16 = 0 \implies (x - 8)(x - 2) = 0 \implies x = 2, 8$ . But 2 is extraneous (it gives us 2 = -2 in the original equation), so solution set is  $\{8\}$ .

**5c**  $\sqrt{x} = \sqrt{x+3} - 1 \implies x = (\sqrt{x+3} - 1)^2 \implies x = (x+3) - 2\sqrt{x+3} + 1 \implies 2\sqrt{x+3} = 4 \implies 4(x+3) = 16 \implies x = 1$ . Solution set:  $\{1\}$ .

**5d** Let  $u = x^2$ , so equation becomes  $4u^2 + 3u - 1 = 0$ , which becomes (4u - 1)(u + 1) = 0 and gives  $u = -1, \frac{1}{4}$ . Now,  $x^2 = -1$  yields  $x = \pm i$ , and  $x^2 = \frac{1}{4}$  yields  $x = \pm \frac{1}{2}$ . Solution set:  $\{\pm i, \pm \frac{1}{2}\}$ .

**5e** |20 - 3x| = 29 implies that  $20 - 3x = \pm 29$ ; then,  $20 - 3x = 29 \implies x = -3$ , and  $20 - 3x = -29 \implies -3x = -49 \implies x = \frac{49}{3}$ . Solution set:  $\left\{-3, \frac{49}{3}\right\}$ .

**6a**  $4x-3 \ge 3x-5 \implies x \ge -2$ , so solution set is  $[-2, \infty)$ .

**6b**  $-18 < x - 4 < 12 \implies -14 < x < 16$ , so solution set is (-14, 16).

**6c**  $6x^2 - 11x - 10 < 0 \implies (3x + 2)(2x - 5) < 0$ . Case 1: 3x + 2 < 0 & 2x - 5 > 0, which leads to a contradiction. Case 2: 3x + 2 > 0 & 2x - 5 < 0, which leads to  $-\frac{2}{3} < x < \frac{5}{2}$ . Solution set:  $\left(-\frac{2}{3}, \frac{5}{2}\right)$ .

**6d**  $2x^3 - 3x^2 - 5x \le 0 \Rightarrow x(2x - 5)(x + 1) \le 0$ . Case 1:  $x \le 0$ ,  $2x - 5 \ge 0$ ,  $x + 1 \ge 0$ , which leads to contradiction. Case 2:  $x \ge 0$ ,  $2x - 5 \le 0$ ,  $x + 1 \ge 0$ , which leads to  $0 \le x \le \frac{5}{2}$ . Case 3:  $x \ge 0$ ,  $2x - 5 \ge 0$ ,  $x + 1 \le 0$ , again contradictory. Case 4:  $x \le 0$ ,  $2x - 5 \le 0$ ,  $x + 1 \le 0$ , which leads to  $x \le -1$ . Solution set:  $(-\infty, -1] \cup [0, \frac{5}{2}]$ .

 $\begin{array}{lll} \textbf{6e} & \frac{10}{2x-3} \leq 5 & \Rightarrow & \frac{10}{2x-3} - \frac{5(2x-3)}{2x-3} \leq 0 & \Rightarrow & \frac{25-10x}{2x-3} \leq 0. \text{ Case 1: } 25-10x \leq 0 \\ \& \; 2x-3 > 0, \text{ which yields } x \geq \frac{5}{2} \; \& \; x > \frac{3}{2}, \text{ and therefore } x \geq \frac{5}{2}. \text{ Case 2: } 25-10x \geq 0 \; \& \\ 2x-3 < 0, \text{ which yields } x \leq \frac{5}{2} \; \& \; x < \frac{3}{2}, \text{ and therefore } x \geq \frac{3}{2}. \text{ Solution set: } \left(-\infty, \frac{3}{2}\right) \cup \left[\frac{5}{2}, \infty\right). \end{array}$ 

**6f**  $|8x - 3| < 4 \implies -4 < 8x - 3 < 4 \implies -1 < 8x < 7 \implies -\frac{1}{8} < x < \frac{7}{8}$ . Solution set:  $\left(-\frac{1}{8}, \frac{7}{8}\right)$ .

7 
$$\sqrt{(-6-8)^2+(5-(-2))^2} = \sqrt{245} = 7\sqrt{5}$$
.

**8**  $(x^2 + 8x + 16) + (y^2 - 6y + 9) = -16 + 16 + 9 \implies (x + 4)^2 + (y - 3)^2 = 3^2$ , which is a circle with center at (-4,3) and radius 3.