Math 120 Fall 2021 Exam 1

- 1. 5 pts. each List the quadrants satisfying each condition.
  - (a) y/x<sup>2</sup> < 0</li>
    (b) x<sup>3</sup> > 0 and y<sup>5</sup> < 0</li>
- 2. 10 pts. Graph  $y = -\frac{1}{2}|x|$ , letting x = -4, -2, 0, 2, 4.
- 3. 10 pts. each Find the solution set of each equation.

(a) 
$$\frac{3}{x+3} = \frac{5}{2x+6} + \frac{1}{x-2}$$
  
(b)  $4x+7 = 7(x+1) - 3x$ 

- 4. 10 pts. Mortimer Lumberbottom invested \$15,000, part of it in a stock that realized a 15% gain. However, the rest of the money invested suffered a 7% loss. If Mortimer had an overall gain of \$1590, how much was invested at each rate?
- 5. 10 pts. Solve  $A = \frac{1}{2}h(a+b)$  for b.
- 6. 10 pts. each Express each in the standard form a + bi.
  - (a)  $(5-2i)^2$ (b)  $\frac{2+4i}{2-i}$
- 7. 5 pts. Do a long division that quickly determines whether  $i^{513}$  equals 1, -1, *i*, or -*i*.
- 8. 10 pts. each Solve each by the method indicated.
  - (a)  $4x^2 13x = -3$  by factoring
  - (b)  $2x^2 4x 1 = 0$  by completing the square
  - (c)  $x^2 2x + 17 = 0$  by the quadratic formula
- 9. 15 pts. A machine produces topless boxes using square sheets of metal. The machine cuts equalsized squares measuring three centimeters on a side from the corners of the sheet, and then folds up the resultant flaps to form the four sides of an open box. If each box must have a volume of 80 cm<sup>3</sup>, find the dimensions of the box.

10. 10 pts. each Solve each equation.

- (a)  $\sqrt{2x-3} \sqrt{x-2} = 1$ (b)  $2x^{2/3} + 7x^{1/3} - 15 = 0$  (a substitution may help) (c) |x+1| + 6 = 2
- 11. 10 pts. each Solve each inequality, stating the solution set in interval notation.
  - (a)  $7 \frac{4}{5}x \le \frac{3}{5}$
  - (b) |2(x-1)+4| < 8
  - (c)  $-3|x+7| \ge -27$