

# MATH 103 EXAM #1 KEY (SUMMER II 2011)

**1a.**  $t - 4 = 6t - 4 \Rightarrow t = 6t \Rightarrow -5t = 0 \Rightarrow t = 0$

**1b.**  $2x + 3x - 12 = 2x - 6 \Rightarrow 5x - 12 = 2x - 6 \Rightarrow 3x = 6 \Rightarrow x = 2$

**2a.**  $4x \leq -32 \Rightarrow x \leq -8$ , so solution set is  $(-\infty, -8]$

**2b.**  $-18 < 3t \leq -12 \Rightarrow -6 < t \leq -4$  so solution set is  $(-6, -4]$

**3.**  $2A = hB + hb \Rightarrow hB = 2A - hb \Rightarrow B = \frac{2A - bh}{h}$

**4.** Letting  $n$  be the number:  $13 - 8n$

**5a.**  $x \leq 6$  and  $x \geq 2 \Rightarrow 2 \leq x \leq 6 \Rightarrow [2, 6]$

**5b.**  $2x < 22$  or  $x > 14 \Rightarrow x < 11$  or  $x > 14 \Rightarrow (-\infty, 11) \cup (14, \infty)$

**6.**  $3x - 7 = 23$  or  $3x - 7 = -23 \Rightarrow 3x = 30$  or  $3x = -16 \Rightarrow x = 10, -16/3$ , so solution set is  $\{-16/3, 10\}$ .

**7.**  $-9 < 2x + 7 < 9 \Rightarrow -16 < 2x < 2 \Rightarrow -8 < x < 1$ , so solution set is  $(-8, 1)$ .

**8a.**  $x$ -intercept is  $(6, 0)$  and  $y$ -intercept is  $(0, -3/2)$ .

**8b.** Omitted.

**9.**  $\left(\frac{-1/2 + 3/2}{2}, \frac{1/3 + 5/3}{2}\right) = (\frac{1}{2}, 1)$

**10.**  $m = \frac{-3 - 2}{9 - 5} = -\frac{5}{4}$

**11.** If  $x$  is the length of the middle side, then:  $x + (x - 75) + (x + 375) = 3075 \Rightarrow 3x = 2775 \Rightarrow x = 925$ . So middle side is 925 miles, short side is 850 miles, and long side is 1300 miles.

**12.** Let  $x$  be the amount invested at 3%, so  $\$24,000 - x$  is the amount invested at 8%. We have  $0.03x + 0.08(24,000 - x) = 1545$ , from which we get  $-0.05x + 1920 = 1545 \Rightarrow -0.05x = -375 \Rightarrow x = 7500$ . Thus \$7,500 was invested at 3%, and \$16,500 was invested at 8%.

**13.** Let  $x$  be the number of liters of 18% alcohol to be added, so  $0.18x + 0.50(20) = 0.30(x + 20) \Rightarrow 0.18x + 10 = 0.30x + 6 \Rightarrow 0.12x = 4 \Rightarrow x = 100/3$ . Thus  $33\frac{1}{3}$  liters of 18% alcohol must be added.

**14.** Slope is  $m = \frac{10 - 5}{-8 - (-2)} = \frac{5}{-6} = -\frac{5}{6}$ , so point-slope formula gives  $y - 5 = -\frac{5}{6}(x - (-2)) \Rightarrow y = -\frac{5}{6}x + \frac{10}{3}$ , which is slope-intercept form. Standard form:  $5x + 6y = 20$ .

**15a.**  $5u^{-8} = \frac{5}{u^8}$

$$\mathbf{15b.} \quad (-2x^9)^5 = -32x^{45}$$

$$\mathbf{15c.} \quad 3v^2(-5v^{-6})(-2v)^0 = 3v^2(-5v^{-6}) = -15v^2v^{-6} = -15v^{-4} = -\frac{15}{v^4}$$

$$\mathbf{15d.} \quad \frac{4a^5(a^{-1})^3}{(a^{-2})^{-4}} = \frac{4a^5a^{-3}}{a^8} = \frac{4a^2}{a^8} = \frac{4}{a^6}$$

$$\mathbf{16.} \quad (2z^2 + 3z - 1) + (4z^2 + 5z + 6) = 2z^2 + 3z - 1 + 4z^2 + 5z + 6 = 6z^2 + 8z + 5$$

$$\mathbf{17.} \quad (9y^2 - 11y + 5) - (4y^2 - 3y + 7) = 9y^2 - 11y + 5 - 4y^2 + 3y - 7 = 5y^2 - 8y - 2$$

$$\mathbf{18a.} \quad (4k + 3)(3k - 2) = 12k^2 - 8k + 9k - 6 = 12k^2 + k - 6$$

$$\mathbf{18b.} \quad (4n + 3m)^2 = (4n + 3m)(4n + 3m) = 16n^2 + 24mn + 9m^2$$

$$\mathbf{18c.} \quad [(m+p)+5][(m+p)-5] = (m+p)^2 - 5(m+p) + 5(m+p) - 5^2 = (m+p)(m+p) - 25 = m^2 + 2mp + p^2 - 25$$