

# MATH 103 EXAM #1 KEY (SPRING 2011)

**1a.**  $t - 4 = 6t - 4 \Rightarrow 5t = 0 \Rightarrow t = 0$

**1b.**  $5x - 12 = 2x - 6 \Rightarrow 3x = 6 \Rightarrow x = 2$

**2a.** Solving gives  $4x \leq -32 \Rightarrow x \leq -8$ , which is the interval  $(-\infty, -8]$

**2b.** Solving:  $-18 < 3t \leq -12 \Rightarrow -6 < t \leq -4$ , which is the interval  $(-6, -4]$

**3.**  $L = \frac{P - 2W}{2}$

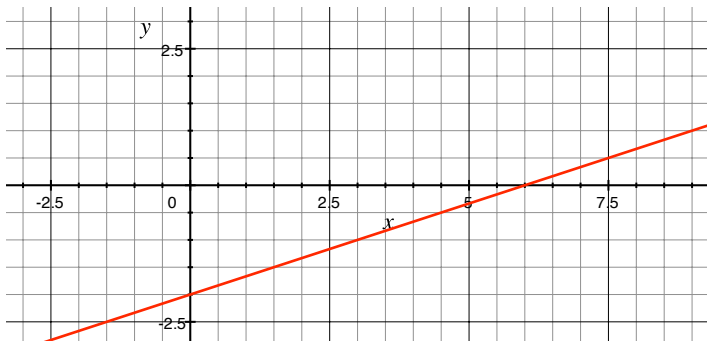
**4.** Letting  $x$  be the number:  $17 - 6x$

**5a.** We get  $x \leq 6$  and  $x \geq 2$ , which can be written  $2 \leq x \leq 6$  and is the interval  $[2, 6]$ .

**5b.** We get  $x < 8$  or  $x > 14$ , which has solution set  $(-\infty, 8) \cup (14, \infty)$ .

**6a.** The  $x$ -intercept is  $(6, 0)$  and the  $y$ -intercept is  $(0, -2)$ .

**6b.**



**7.** By the Midpoint Formula:  $\left( \frac{-\frac{1}{2} + \frac{3}{2}}{2}, \frac{\frac{1}{3} + \frac{5}{3}}{2} \right) = \left( \frac{1}{2}, 1 \right)$

**8.**  $m = \frac{2 - (-3)}{5 - 9} = -\frac{5}{4}$

**9.** If  $x$  is the length of the middle side, then:  $x + (x - 75) + (x + 375) = 3075 \Rightarrow 3x = 2775 \Rightarrow x = 925$ . So middle side is 925 miles, short side is 850 miles, and long side is 1300 miles.

**10.** Let  $x$  be the number of dollars invested at 3%, so  $12,000 - x$  is the amount invested at 5%. Then, tallying interest amounts from each investment, we get  $0.03x + 0.05(12,000 - x) = 440$ . Solving this equation yields  $x = 8,000$ . So \$8,000 was invested at 3%, and \$4,000 at 5%.

**11.** Equate the number of liters of pure alcohol, letting  $x$  be the number of liters of 14% solution to be added:  $0.14x + 0.50(20) = 0.30(x + 20)$ . Solving yields  $0.16x = 4$  and finally  $x = 25$ . Thus 25 liters of 14% solution must be added.